

Figure 1: Basic Network

# Seminar 5: Exercises

## Exercise 1

An application generates a data flow with the following characteristics:

- $\lambda_1 = 1000$  packets/second, following a Poisson process.
- Average packet size of  $E[L_1] = 8500$  bits.
- The packet size distribution is characterized by a  $CV[L_1] = 3.2$ .

This data flows is send through a network interface that is connected to a wireless link of capacity  $R = 10$  Mbps. We can consider the buffer space is large enough to consider it infinite.

1. Calculate the time a packet of such an application remains in the system  $E[D_1]$ .
2. If the network interface is shared with another application that injects  $\lambda_2 = 100$  packets/second to the network interface, where the packets are of constant size and equal to  $L_2 = 8000$  bits, calculate the new value of  $E[D_1]$ , and the value of  $E[D_2]$ .

## Exercise 2

Let us consider a network interface that receives  $\lambda = 20000$  packets/second following a Poisson process. The probability distribution (histogram) of the packet sizes is as follows:

- Packets of  $L_1 = 64$  Bytes with probability 0.3
- Packets of  $L_2 = 500$  Bytes with probability 0.5
- Packets of  $L_3 = 1500$  Bytes with probability 0.2

The network interface has a large buffer space which can be considered infinite and is able to transmit packets at  $R = 100$  Mbps.

1. Calculate the average delay a packet remains in the buffer ( $E[D_q]$ ) and in the system ( $E[D]$ ) if we make the assumption that packets are exponentially distributed with average  $E[L] = 0.3L_1 + 0.5L_2 + 0.2L_3$  bits.
2. Calculate the traffic load ( $a$ ) in Erlangs, and which fraction corresponds to packets of size  $L_1$ ,  $L_2$  and  $L_3$  respectively (i.e.,  $a_1$ ,  $a_2$ , and  $a_3$ ).

3. Considering the actual packet size distribution, calculate the average residual time ( $E[D_r]$ ). Compare this value with the residual time in case the packet sizes follow an exponential distribution.
4. Considering the actual packet size distribution, calculate the  $E[D_q]$  and  $E[D]$ ,  $E[D_1]$ ,  $E[D_2]$  and  $E[D_3]$  delays, where  $E[D_i]$  is the time a packet of size  $i$  remains inside the network interface. Compare the results with the values obtained assuming the packet sizes where exponentially distributed.

*Hint:*  $E[D_s^2] = 2E^2[D_s]$  in the case of M/M/1.

### Exercise 3

Let us consider an AP transmitting a data flow of  $B = 4$  Mbps to a station placed at a distance of  $d = 25$  meters. All the packets of the flow have the same fixed size of  $L = 1100$  bits (deterministic), and packets arrive to the buffer following a Poisson process. The network interface at the AP has an infinite buffer size. The propagation delay is negligible, as well as any packet processing delay. The transmission delay is  $E[D_s] = 0.195$  ms.

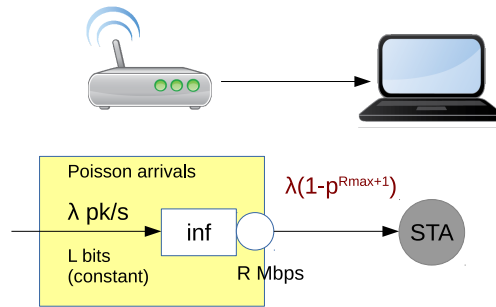


Figure 2: An AP transmitting a data flow to an STA

1. Calculate the delay  $E[D]$  of the packets in the AP if the packet error probability is  $p = 0$ .
2. Calculate the delay  $E[D]$  of the packets in the AP if the packet error probability is  $p = 0.2$  and  $R_{\max} = 1$ .
3. Calculate the delay  $E[D]$  of the packets in the AP if the packet error probability is  $p = 0.2$  and  $R_{\max} = 3$ .
4. Calculate the throughput in bits / second for all 3 previous cases ( $\lambda L(1 - p^{R_{\max}+1})$ ).
5. Explain the effects of  $p$  and  $R_{\max}$  in the delay and throughput.

## Solution Exercise 1

```
lambda1 = 1000;
```

```
EL1 = 8500;
```

```
CVL1 = 3.2;
```

```
R=10E6;
```

```
% a)
```

```
EDs1 = EL1 / R;
```

```
ED2s1 = EDs1^2*(1+CVL1^2);
```

```
a1 = lambda1*EDs1;
```

```
disp('Only flow1')
```

```
EDr = lambda1*ED2s1/2;
```

```
ED1 = EDr/((1-a1)) + EDs1
```

```
% b)
```

```
lambda2 = 100;
```

```
CVL2 = 0;
```

```
EL2 = 8000;
```

```
lambda = lambda1+lambda2;
```

```
p1 = lambda1/lambda;
```

```
p2 = lambda2/lambda;
```

```
EDs2 = EL2/R;
```

```
a2 = lambda2 * EDs2;
```

```
ED2s2 = EDs2^2*(1+0);
```

```
EDr1 = lambda1*ED2s1/2;
```

```
EDr2 = lambda2*ED2s2/2;
```

```
% EDr = lambda/2 * (p1*D2s1 + p2*D2s2)
```

```
disp('With traffic 2')
```

```
EDr = lambda *(p1*ED2s1 + p2*ED2s2)/2
```

```
a=a1+a2
```

```
EDq = EDr/(1-a)  
ED1 = EDS1 + EDq  
ED2 = EDS2 + EDq  
ED2
```

## Solution Exercise 2

```
%% EX2  
% 1)
```

```
L1=64*8;  
L2=500*8;  
L3=1500*8;
```

```
lambda=20E3;
```

```
R=100E6;
```

```
EL = 0.3*L1 + 0.5*L2 + 0.2*L3;
```

```
mu = R/EL;
```

```
disp('ED M/M/1');  
ED = 1 / (mu - lambda)  
EDq = ED - 1/mu
```

```
%2
```

```
EDs = EL/R;
```

```
a = lambda*EDs;
```

```
a1 = 0.3*lambda*L1/R;  
a2 = 0.5*lambda*L2/R;  
a3 = 0.2*lambda*L3/R;
```

```
%3
```

```
disp('Residual Times');
```

```

EDs1 = L1/R;
EDs2 = L2/R;
EDs3 = L3/R;

ED2s = 0.2*EDs1^2 + 0.5*EDs2^2 + 0.2*EDs3^2;

EDr = lambda * ED2s/2

%ED2s_expo = 2*EDs^2;
%EDr_expo = lambda*ED2s_expo/2

% 4 -----

disp('ED M/G/1');

EDq = EDr / (1-a)
ED = EDq + EDs
ED1 = EDq + EDs1
ED2 = EDq + EDs2
ED3 = EDq + EDs3

```

### Solution Exercise 3

```

function Exercise3()

L = 1100;
R = 26E6;
T = 40E-6 + (240+L)/R + 16E-6 + 40E-6+112/R + 34E-6+9E-6

B=4E6;
lambda = B/L;

% ----- p = 0

EDs = T
ED2s = EDs^2*(1+0^2)
a = lambda * EDs

EDq = lambda * ED2s / (2*(1-a))
ED = EDs + EDq

S = lambda*L

```

```

%EDs = 1.9485e-04
%ED2s = 3.7965e-08
%a = 0.70853
%EDq = 2.3683e-04
%ED = 4.3167e-04

% ----- p = 0.2, Rmax = 1

p=0.2

p1 = (1-p);
p2 = p;

EDs = p1*T + p2*2*T
ED2s = p1*T^2 + p2*(2*T)^2

a = lambda * EDs

EDq = lambda * ED2s / (2*(1-a))
ED = EDs + EDq

S = lambda*L*(1-p^2)

%p = 0.20000
%EDs = 2.3382e-04
%ED2s = 6.0744e-08
%a = 0.85024
%EDq = 7.3746e-04
%ED = 9.7128e-04

% ----- p = 0.2, Rmax = 3

p1 = (1-p);
p2 = p*(1-p);
p3 = p*p*(1-p);
p4 = p*p*p;

EDs = p1*T + p2*2*T + p3*3*T + p4*4*T
ED2s = p1*T^2 + p2*(2*T)^2 + p3*(3*T)^2 + p4*(4*T)^2

a = lambda * EDs

EDq = lambda * ED2s / (2*(1-a))

```

```
ED = EDs + EDq
```

```
S = lambda*L*(1-p^4)
```

```
%EDs = 2.4317e-04
```

```
%ED2s = 7.0463e-08
```

```
%a = 0.8842
```

```
%EDq = 0.0011
```

```
%ED = 0.0013
```

```
% Throughput
```

```
%p= 0; S = 4000000
```

```
%p= 0.2; Rmax = 1; S = 3840000
```

```
%p= 0.2; Rmax = 3; S = 3993600
```

```
end
```