Macroeconomic Experiments (my take)

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Outline of this lecture

- Four illustrations (examples of topics that one could study):
 - Growth Models
 - Multiple Equilibria and Poverty Traps
 - DSGE economies
 - International Economies
- All four have features that:
 - Stick close to an existing theoretical model
 - Easier to communicate
 - Have hypotheses and benchmark predictions that come from a model
 - Have a specific research question as a focus

The experimental approach to testing theories



The experiment specifies the structure of the economy, and observes behavior and outcomes.

Theoretical models specify structure and behavior, and study outcomes

Application I: Dynamic Economies; Testing Growth Models

- Reference (Lei and Noussair, 2002)
- Most experiments consist of repetition of a stationary environment with no dynamic link between periods.
- Macroeconomic models directly focus on intertemporal linkages between variables, such as between savings and future consumption.
- This experiment illustrates one way intertemporal design issues can be approached.

Theoretical Model: The Ramsey/Cass/Koopmans Model of Optimal Growth

• A representative consumer in the economy has a lifetime utility given by

$$\sum_{t=0}^{\infty} (1+\rho)^{-t} U(C_t)$$

• ρ is the discount rate, C_t is the quantity of consumption at time t, and $U(C_t)$ is the utility of consumption. The economy faces the resource constraint:

$$C_t + K_{t+1} \le A * F(K_t) + (1 - \delta)K_t$$

- δ is the depreciation rate, K_t is the economy's aggregate capital stock at the beginning of period *t*, and *A* is an efficiency parameter on the production technology.
- Under the assumption that the production function is concave, the principal predictin of the model is that C_t and K_t converge asymptotically to optimal steady state levels.
- The optimal steady state given by the solution to:

 $C^*=F(K^*)-\delta K^*$

 $K^* = \rho + \delta$

- The behavior of this economy (in theory) can be interpreted as:
 - The solution to an optimization problem of a benevolent social planner
 - The rational expectations equilibrium of a decentralized market economy
- The experiment considers two issues:
- 1) Do economies with this structure convergence to the optimal steady state?
- 2) How important is the institutional structure to obtain convergence to the optimal steady state?

Parameters and Predictions

- U(C) = 310C 5C² (given to subjects on sheet of paper, with marginal values indicated, rounded to integer values)
- F(k) = 6.96k^{.5} (on sheet of paper, marginal productivity indicated, rounded to integer values)
- δ = 1 (embedded into production function, limit the number of new concepts, why make people learn what depreciation is if you don't have to)
- ρ = 1/9 (round number, 1 in 10 chance the game will end in each period, expected horizon 10 rounds)
- C* = 12
- K* = 10

Result: If individuals are given incentives to solve the dynamic optimization problem, it is very difficult. Social Planners starting with endowment of 20 units:



Figure 6: Time Series of Consumption: Social Planners High Endowment

Suppose a team of five people is making the decision instead. They still have a lot of trouble







Suppose the Model is Interpreted and Implemented as a Decentralized Economy.

- There are five agents in the economy
- The economy's production capability and utility function is divided up among the five agents.
- Agents are not symmetric. Their utility and production functions differ. This asymmetry ensures that gains from trade exist from the exchange of capital (we want to have an active market).
- A market is available to exchange capital (using double auction rules, because a competitive model is being tested).
- There is money, an experimental currency, in the economy, which agents use for purchases and sales of capital. The money is not fiat money, but is convertible into dollar earnings for participants (this means that tradeoff between marginal values and price is easier).

Timing within a period t

- At the beginning of period *t*, production occurs mapping k_t into output ($c_t + k_{t+1}$)
- A double auction market for output is open for two minutes in which they can exchange output.
- Agents have one minute to allocate any portion of their output to consumption c_t
- At the beginning of period *t+1*, production occurs mapping k_{t+1} into output (c_{t+1} + k_{t+2}).
- A common issue that arises in macroexperiments is the lack of explicit timing in macroeconomic models.

Timing within a period



Timing of sessions (ending a session)

- A *horizon* refers to the entire life of an economy.
- A *session* refers to a single day's activity in the laboratory.
- How do you end an infinite horizon economy?
- Implementation of infinite horizon with discounting: In each period, there was a 10% probability that the horizon would end.
- If a horizon ended with more than one hour to go in the session, a new horizon was started.
- If a horizon still had not ended at the scheduled end of the session, the horizon would be continued on another evening.

- Subjects would have the option of continuing in their roles in the continued session.
- If they chose not to continue, a substitute would be recruited to take her place. The original subject would also receive the money earned by the substitute.

Results: Consumption patterns in the decentralized economy



Summary of results

- When individuals are presented with the social planner's optimization problem, the economies perform poorly.
- Institutions have an impact on the level and variance of output and on welfare
- The decentralized market economy converges to the optimal steady state.
 - The key appears to be the existence of an endogenous market price for capital revealing it's scarcity.

Application II: Multiple Equilibria in Dynamic Economies (source is Capra et al., 2009)

- The existence of multiple equilibria can (theoretically) explain differences in income between countries, even if they have identical institutions (Rosenstein-Rodan, 1943; Murphy et al., 1989; Azariadis, 1990; Galor and Zeira, 1993; Ray, 2003).
- Unfortunate countries may find themselves in an inferior equilibrium, a "poverty trap".
- Institutions may play a role if multiple equilibria exist. Some institutions may facilitate successful coordination on better equilibria.

An environment with multiple equilibria

- Suppose that there exist two stable equilibria, which are Pareto-ranked so that the inferior equilibrium represents a poverty trap.
- The value of the productivity parameter A depends on the economy's capital stock. There exists a threshold level of capital stock, above which A has a higher value.

$$A = \begin{cases} \underline{\underline{A}}, & \text{if } K < \hat{K} \\ \overline{\underline{A}}, & \text{if } K \ge \hat{K} \end{cases}$$

Parameters of the Experiment

• The economy-wide production technology is an approximation

of $F(K_t) = 7.88 * K_t^{0.5}$ for $K_t < 31$

and of $F(K_t) = 16.771 * K_t^{0.5}$ for $K_t \ge 31$

- This is the easiest way, in terms of subject comprehension to create multiple equilibria.
- The economy wide utility function is an approximation of $U(C_t) = 400C_t - 2(C_t)^2$
- Discount rate ρ = 0.25
- Depreciation rate of Capital $\delta = 1$
- The initial endowment of capital is 5 for each agent, for a total of 25.

Production function includes threshold externality



Theoretical Predictions

- There is an optimal steady state in which (C*, K*) = (70,45)
- From any initial level of capital stock, optimal decisions (of a benelovent social planner) at each point in time imply monotonic convergence to (C*, K*).
- However, if the economy is decentralized, there are two stationary rational expectations competitive equilibria at (C^H, K^H, p^H) = (70,45,118) and (C^L, K^L, p^L) = (16,9,334)
- **RESULT:** The decentralized economy converges to the poverty trap.

Results: Observed and Equilibrium Aggregate Consumption (Five Sessions) C* optimal = 70, C* poverty trap = 16

Vertical axes: aggregate consumption

Horizontal axes: time

Breaks in series: New horizon beginning

Results:

No economy surpasses the capital stock threshold.

Convergence to near poverty trap is typical outcome

§= Each data point represents a period in a horizon. Horizons are separated by spaces

Observed Welfare and Capital Stock in Comparison to Poverty Trap and Optimum

Research question: What institutions can improve on these outcomes?

- This parametric structure provides a challenging environment for additional institutions to avoid/exit the poverty trap.
- We consider whether two institutions, communication and voting, alone or together, can improve outcomes in this economy.
 - Voting is a stylized version of "democracy" and
 - Communication is a stylized version of "freedom of expression (free press)",

The Communication treatment

- Identical to the baseline treatment, except that before the market opened, subjects were allowed to communicate with each other.
- Each agent's screen displayed a chat-room, which they could use to send and receive messages in real time.
- Communication was unrestricted and all agents could observe all messages.

Observed and Equilibrium Aggregate Consumption, Communication Treatment; C* optimal = 70, C* inferior = 16

Vertical axes: aggregate consumption

Horizontal axes: time

Breaks in series: New horizon beginning

Results: Individual sessions converge to near one of the equilibria.

However, which equilibrium it converges to varies between sessions.

Example of how institutional structure affects mean and variance of income.

The Voting treatment

- Identical to the baseline treatment except that consumption and investment decisions were determined in the following manner:
- Two agents were randomly chosen in each period to make proposals on how much each agent in the economy should consume.
- Before submitting proposals, proposers received information indicating the current stock of capital held by each agent.
- Proposals were followed by majority voting. All agents were required to vote in favor of exactly one of the two proposals.
- The proposal that gained at least 3 (of the 5 total) votes became binding. Each agent consumed the quantity of output specified under the winning proposal, and began next period with the amount of capital allotted to her under the winning proposal.

Submitting Proposals

	Results in stage 1 :	Units of K at starting 12	K in the Economy 39	Cash endowment 10000	Market Price	K sold	Cash transferred 396	Cash after trading 10396
History	Your limit prices (for K=1, K=2 and so on)	99*99*99*99*99*99*9	99*99*99*99*99*9	9*99*99*				
	All players' limit prices (for each K, its price and its proposer)	(1,99,4);(2,99,5); <	;(3,99,1);(4,99,2);	(5,99,3);(6,99,4);(7	`,99,5);(8,99,1);(9	99,2);(10,99,3);(11,99	9,4);(12,99,5);(13,99	,1);(14,99,2);(15,99 •
				You are pl	ayer 1			
	Current K	Player 1 8	Player 2	Play	yer 3 7	Player 4	Player 5	
	You a	and another v	vere randoi Current K	mly chosen Lis colored in	to make a p n blue.	eoposal. Your		
				Validate				
	Enter 5 numbers i	ndicating the į	proposed qu	antity of Unit	s Remaining	as K for each	player.	
	For each playe	er the number	must be les	s than or equ as K must be	al to the uni less than 3	ts of K current	ly and the	

Submitting Votes

	Results in stage 1 :	Units of K at K in the starting Economy 12 39	Cash y endowment 10000	Market Price 99	K sold	Cash transferred 396	Cash afte trading 10396
listory	Your limit prices (for K=1, K=2 and so on)	99*99*99*99*99*99*99*99*99*99	99*99*99*99*				
	All players' limit prices (for each K, its price and its proposer)	(1,99,4);(2,99,5);(3,99,1);(4,99	1,2);(5,99,3);(6,99,4);(7	7,99,5);(8,99,1);(9,99	ı,2);(10,99,3);(11,99,4 <u>)</u>);(12,99,5);(13,99,1);(14,99,2);(15
			10	u are player i			
	Inite Romaining as K	Player 1 Player 2	Player 3	Player 4	Player 5	Your \	/ote
	under Proposal 1		1	1		Propo	osal 1
	Units Remaining as K under Proposal 2	1 2	1	1	1	Propo	osal 2
	Choose you	Your possible Units Re r preference by clicking (emaining as K on Proposa 1 o	are colored in r 2 and validate	b lue. 9 your choice.	Valio	date

Observed and Equilibrium Aggregate Consumption, Voting Treatment

C* optimal = 70, C* inferior = 16

Results:

-In most sessions, economy escapes poverty trap

- High variance from one period to the next within

The hybrid treatment: Both communication and voting are present Timing in the hybrid treatment

Observed and Equilibrium Aggregate Consumption, Hybrid Treatment; C* optimal = 70, C* inferior = 16

Horizontal axis: time

Breaks in series: New horizon beginning

Result; The addition of voting and communication allows the economy to escape poverty trap in all sessions.

Results

- Baseline: The economies of the baseline treatment converge to near the poverty trap. Does not escape poverty trap in any session.
- **Communciation**: The economies of the communication treatment converges to close to one of the stationary equilibria. However, the one it converges toward varies between sessions. Probability of avoiding the poverty trap greater than under baseline.
- **Voting**: The voting treatment exhibits variable behavior from one period to the next. Probability of avoiding the poverty trap greater than under baseline.
- Hybrid: Also shows variable behavior from one period to the next. Escapes the poverty trap in all sessions.

Application III: DSGE models

- Construct an experimental New Keynesian DSGE macroeconomy, populated with human agents.
- Three types of (infinitely lived) agents
 - Consumers: supply labor, purchase (3) products, and save for the future
 - Producers: purchase labor, produce one of the (3) products, sell output
 - Central bank: sets interest rates
- Preferences and productivity subject to shocks

Producer incentives

• Maximize profit:

$$\Pi_{it} = p_{it}y_{it} - w_t L_{it}$$
$$y_{it} = A_t L_{it}$$
$$A_t = A_0 + \gamma A_{t-1} + \delta \varepsilon_t$$

Where

 $\Pi_{it} = \text{profit of firm i in period t}$ $p_{it} = \text{price of good i in period t}$ $y_{it} = \text{production of good i in t}$ $w_t = \text{wage in t}$ $L_{it} = \text{labor bought by i in t}$ $A_t = \text{productivity parameter in t}$ $\varepsilon_t = \text{productivity shock in t}$ $\gamma = 0.8, \delta = 0.2, A_0 = 0.7$

Consumer incentives

- Payoff in period t of consumer $j = \beta^t [U_{jt}(C_{jt}) D_j(L_{jt})]$
- $U_{jt}(C_{jt}) = \sum_{i} h_{ijt} [c_{ijt}^{(1-\sigma)}/(1-\sigma)]$
- $h_{ijt} = \mu_{ij} + \tau h_{ijt-1} + \delta \varepsilon_{jt}$
- $D(L_{jt}) = d^* L_{jt}^{1+\eta} / (1+\eta)$
- Where

C_{it}= consumption at time t of consumer j

 L_{jt} = labor supplied at t

 $D_j(L_{jt})$ = disutility to j of labor he supplies at t

 c_{ijt} = consumption of good i by consumer j at t

 ε_{jt} = preference shock for consumer j in period t

 β = .99, μ_{ij} = 120, τ = 0.8, d = 15, η = 2, n = 3.

Consumer incentives

• Faces a budget constraint:

 $w_t L_{jt} + 1/n \sum_i \Pi_{i,t-1} + (1 + r_t) s_{j,t-1} = \sum_i p_{it} c_{ijt} + s_{jt}$

- s_{jt} can be thought of as savings or bonds
- Create monopolistic competition with different preference shocks for each good.

Experimental Design

- Timing within a period
- Stage 1: Labor market
 - There is a shock to productivity at the beginning of each period.
 - A double auction market operates for labor.
 - Cost of supplying labor and productivity is (privately) known at the time of trade.
 - Sales take place in terms of (fiat) experimental currency. Costs of labor supply are incurred in terms of utility (Euros).
- Production occurs automatically
 - Each producer has available a quantity of his product to sell for stage 2

Labor market: Consumer

Labor Market: Producer

Stage 2 of a period: Product market

- There is a shock to consumer preferences.
- Sellers post prices
- Buyers purchase units of each of the three products at their own pace
 - Product transactions take place in terms of (fiat) experimental currency
 - Valuations are in terms of utility (Euro paid to the subjects)
 - It is possible that some units will go unsold, or that stock will have been depleted at the time a consumer wants to buy.

Product market: Producer

Product Market: Consumer

Savings, producer profit, discounting, and ending the experiment

- Consumers' unspent cash is saved for later periods, and earns interest.
- Producers' unspent cash (profit) is awarded to the consumers in equal shares.
 - However, the agents acting as producers received a payment in Euro equal proportionally to their profits. The payment was corrected for inflation.
- The game goes at least 50 periods, randomly stopping between periods 50

 70.
- Utility (euro earnings) from consumption and labor supply exhibit a decreasing trend of 1% per period.
- The final cash balance of consumers is "bought out" by the experimenter.
- Interest rate set by an instrumental rule:

 $r_t = \pi^* + 1.5(\pi_{t-1} - \pi^*), \pi^* = .03$

where, π_t = inflation in period t, π^* = inflation target

Timing of a session

- A session took $3\frac{3}{4} 4\frac{3}{4}$ hours.
- Instructions read (~30 minutes)
- 5 period practice economy (~30 minutes)
- > 50 period economy that counted toward earnings.
- Placed bounds on wages and prices for the first two periods.

The treatments

• (1) Baseline

The conditions described above

• (2) Human Central Banker:

In each period, three agents each chose an interest rate. The group's decision (and thus the rate in effect) was the median of the three choices.

The agents had an incentive to minimize the loss function Loss_t = $(\pi_t - \pi^*)^2$

Central bankers were paid an amount equal to max{0, a – b*Loss}

• (3) Menu Cost:

- To change the price from one period to the next, producers had to pay a cost equal to: $0.025*p_{i,t-1}*y_{it}$
- Otherwise identical to Baseline

• (4) Low Friction

- Perfect, rather than monopolistic, competition.
- Valuations are the same for each good ($\mu_{ij} = \mu_0$), though differ by individual and by time period ($\epsilon_{it} > 0$).
- This means that the goods are perfect substitutes.
- Otherwise identical to Baseline
- Parameters set to equate welfare to Baseline under a simulation we conducted.

Treatments

	Monopolistic Competition	Human central banker	Menu cost for product price change (= .025[p _{i,t-1} *y _{it}])
Baseline	Y	N	N
Menu cost	Y	N	Y
Human central banker	Y	Y	N
Low friction	N	N	N

Procedures

- 16 sessions, four under each treatment
- 3 producers and 3 consumers in each session
- In the Human Central Banker treatment, there were also three central bankers.
- Subjects were undergraduates at Tilburg University
- Experiments conducted in English
- Average earnings = 43.99 euro

Hypothesis

- Persistence of shocks (effect beyond the current period):
 - Treatment differences
 - In treatments Baseline, Human Central Banker, and Low Friction no persistence, in treatment Menu Cost, shocks are persistent (both Menu Cost and market power are needed for persistence in New Keynesian DSGE model).
 - Empirical stylized fact is that a shock to interest rates, output, or inflation, has persistent effects on itself and on some of the other two variables.
- Also can compare between treatments
 - GDP, inflation, welfare, employment, etc...

Results: GDP

GDP is highest under Low Friction

GDP is lowest in the late periods under Human Central Banker

Menu Costs do not affect GDP

Results: Inflation

Inflation rate is similar on average in all four treatments, including Human Central Bankers Volatility is lowest under Menu costs Volatility is highest under Human Central Banker

A degree of heterogeneity exists within each treatment

Treatment differences

- Very little persistence in the Low Friction treatment.
- More persistence in Menu Cost than in Baseline
- Less persistence in Human Central Banker than in the Baseline treatment

Conclusions

- Methodology
 - It is feasible to construct a DSGE model in the laboratory. It is possible to verify stylized facts, check assumptions, and potentially test policy prescriptions.
- Persistence
 - Monopolistic competition, in conjunction with multiple agents and bounded rationality, is sufficient to generate persistence
 - Menu costs increase persistence.
 - Negligible persistence in Low Friction, under perfect competition.
 Biases in decision making do not generate the required persistence.

Application IV: Multiple Market "International" Economy (Noussair et al., 2007).

- Consider a larger scale and more complex economy.
- 60 subjects divided into three countries of population 20.
- Trade in each country takes place in terms of its own currency.
- There are two inputs, V and W residing in each country.
- There are three outputs X, Y, and Z, all of which can be produced in all three countries from inputs V and W from the same country.
- Multiple inputs are required to produce each output. Production is Cobb-Douglas $f(v,w) = Av^{25} w^{25}$, with A equaling either 2 or 4.
- 21 markets: 6 input, 9 output, and 6 currency markets.
- The research question: Can an economy this complex converge to its competitive equilibrium?
- Note: Existence theorem for CE does not apply when demand is discrete and there are multiple markets. To parameterize, specify prices and then fit demand and supply curves and production functions.

Subjects' roles

- There are three roles agents can have in the economy
 - Suppliers: sellers of V and W.
 - Producers: buyers of V and W, producers of X, Y, or Z from V and W, sellers of X, Y, or Z
 - Consumers: buyers of X, Y, and Z. Demand for outputs is separable and linear
- Individual subjects typically have more than one role (this conserves subjects. No individual could be on two sides of same market).
- The experiment is done over two or three days, 9 hours total (4 hours seems to be the daily limit).
- 1 hour instructions, 2 hours practice, 6 hours of data acquisition.
- The environment is stationary. No intertemporal links.

Structure of the economy

Running complex experiments

- Don't ask individual subject to do too much
- Divide instructions into modules for different individuals.
- Be patient, people's understanding improves fast.
- Have many practice periods
- Include decision support information.
- Minimize number of new concepts

Display as seen by subjects

Production Screen

View Your Production Table

				_			
		Past Usage	Current Inventory	Production Plan	Expected Product	New Total	
	x		0		0	0	x
Outputs	y		0		0	0	y
	z		0		0	0	z
Innuts	v	0	0	0		0	v
inputs	w	0	0	0		0	w

View Your **Production Table**

Production Function: Isoquants

Table of Production of X, Y, or Z from V and W

Production Page

V used	Amount produced																									
20	0	8	10	11	12	13	13	14	14	15	15	15	16	16	16	17	17	17	17	18	18	18	18	19	19	19
19	0	8	10	11	12	12	13	14	14	14	15	15	16	16	16	16	17	17	17	17	18	18	18	18	18	19
18	0	8	10	11	12	12	13	13	14	14	15	15	15	16	16	16	16	17	17	17	17	18	18	18	18	18
17	Ο	8	10	11	11	12	13	13	14	14	14	15	15	15	16	16	16	16	17	17	17	17	18	18	18	18
16	0	8	10	11	11	12	13	13	13	14	14	15	15	15	15	16	16	16	16	17	17	17	17	18	18	18
15	0	8	9	10	11	12	12	13	13	14	14	14	15	15	15	15	16	16	16	16	17	17	17	17	17	18
14	0	8	9	10	11	12	12	13	13	13	14	14	14	15	15	15	15	16	16	16	16	17	17	17	17	17
13	Ο	8	9	10	11	11	12	12	13	13	14	14	14	14	15	15	15	15	16	16	16	16	16	17	17	17
12	0	7	9	10	11	11	12	12	13	13	13	14	14	14	14	15	15	15	15	16	16	16	16	16	16	17
11	0	7	9	10	10	11	11	12	12	13	13	13	14	14	14	14	15	15	15	15	15	16	16	16	16	16
10	Ο	7	8	9	10	11	11	12	12	12	13	13	13	14	14	14	14	14	15	15	15	15	15	16	16	16
9	Ο	7	8	9	10	10	11	11	12	12	12	13	13	13	13	14	14	14	14	14	15	15	15	15	15	15
8	Ο	7	8	9	10	10	11	11	11	12	12	12	13	13	13	13	13	14	14	14	14	14	15	15	15	15
7	Ο	7	8	9	9	10	10	11	11	11	12	12	12	12	13	13	13	13	13	14	14	14	14	14	14	15
6	Ο	6	7	8	9	9	10	10	11	11	11	11	12	12	12	12	13	13	13	13	13	13	14	14	14	14
5	Ο	6	7	8	8	9	9	10	10	10	11	11	11	11	12	12	12	12	12	12	13	13	13	13	13	13
4	Ο	6	7	7	8	8	9	9	10	10	10	10	11	11	11	11	11	11	12	12	12	12	12	12	13	13
3	0	5	6	7	7	8	8	9	9	9	9	10	10	10	10	10	11	11	11	11	11	11	11	12	12	12
2	0	5	6	6	7	7	7	8	8	8	8	9	9	9	9	9	10	10	10	10	10	10	10	10	11	11
1	0	4	5	5	6	6	6	7	7	7	7	7	7	8	8	8	8	8	8	8	8	9	9	9	9	9
0	Ο	0	0	Ο	Ο	Ο	0	0	Ο	0	0	Ο	Ο	0	Ο	Ο	Ο	Ο	Ο	0	Ο	Ο	Ο	Ο	Ο	Ο
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
													Wυ	sed												

Individual roles, demand, supply and production functions

Туре	Country	Role	Parameter values	# In exp 1
1	A	Producer of X Consumer of Y	$ \begin{aligned} f_x^A(k,l) &= 4l^{0.25}k^{0.25} \\ U(y) &= 1650y{-}100y^2 \end{aligned} $	5
2	A	Producer of Y Consumer of X and Z	$ \begin{split} f_y^A(k,l) &= 2l^{0.25}k^{0.25} \\ U(x,z) &= 700x\!-\!100x^2 + 1900z\!-\!100z^2 \end{split} $	5
3	A	Producer of Z Consumer of X and Y	$ \begin{aligned} f_z^A(k,l) &= 2l^{0.25}k^{0.25}\\ U(x,y) &= 700x\!-\!100x^2\!+\!1650y\!-\!100y^2 \end{aligned} $	5
4	A	Supplier of L and K Consumer of Z	$\begin{split} C(l,k) &= 26l + 2l^2 + 10k + 5k^2 \\ U(z) &= 1900z {-}100z^2 \end{split}$	5
5	В	Producer of X Consumer of Y and Z	$ \begin{aligned} f_x^{B}(k,l) &= 2l^{0.25}k^{0.25}\\ U(y,z) &= 3900y{-}400y^2{+}5600z{-}400z^2 \end{aligned} $	5
6	В	Producer of Y Consumer of X	$f_y^B(k,l) = 4l^{0.25}k^{0.25}$ $U(x) = 3800x - 400x^2$	5
7	В	Producer of Z Consumer of X and Y	$ \begin{split} f^B_Z(k,l) &= 2l^{0.25}k^{0.25}\\ U(x,y) &= 3800x{-}400x^2{+}3900y{-}400y^2 \end{split} $	5
8	В	Supplier of L and K Consumer of Z	$\begin{array}{l} C(l,k) = 48l + 15l^2 + 55k + 7.5k^2 \\ U(z) = 5600z - 400z^2 \end{array}$	5
9	С	Producer of X Consumer of Y and Z	$ \begin{split} f^C_x(k,l) &= 2l^{0.25}k^{0.25}\\ U(y,z) &= 13500y\!-\!1000y^2\!+\!16000z\!-\!1000z^2 \end{split} $	5
10	С	Producer of Y Consumer of X and Z	$\begin{split} f_y^C(k,l) &= 2l^{0.25}k^{0.25}\\ U(x,z) &= 12000x - 1000x^2 + 16000z - 1000z^2 \end{split}$	5
11	С	Producer of Z	$f_z^C(k, l) = 4l^{0.25}k^{0.25}$	5
12	С	Supplier of L and K Consumer of X and Y	$\begin{split} C(l,k) &= 300l + 50l^2 + 220k + 20k^2 \\ U(x,y) &= 12000x - 1000x^2 + 13500y - 1000y^2 \end{split}$	5

Results: Nominal output prices compared to equilibrium levels

Fig. 4. Output prices in the three counties, experiment 3.

Input prices and equilibrium levels

Fig. 5. Input prices in the three countries, experiment 3.

The exchange rate in comparison to equilibrium and Purchasing Power Parity levels: PPP is supported

Fig. 6. Observed, equilibrium and PPP exchange rates, experiment 3.

Overall conclusions from complex economies

- Equilibration, convergence to competitive equilibrium with decreasing variance, is observed.
- The equilibration process appears to be slower, the more complex the economy.
- It is feasible to construct and implement very complicated economies in the laboratory.

• I'll stop here: Any questions?